

**CORRECTIONS TO “ON QUANTUM UNIQUE
ERGODICITY FOR $\Gamma \backslash H \times H$ ”**

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We note that (**) on page 920 of [1], as well as its derivation on page 921, has a sign error. In fact, and this will actually be useful for us later, one can in addition improve the error estimate: as we shall show for $-N \leq l, m, k, t \leq N$ with $N < r_1/2$

$$\langle f\phi_{2l,2m}, \phi_{2k,2t} \rangle = \langle f\phi_{2l+2,2m}, \phi_{2k+2,2t} \rangle + O_f(r_1^{-1}). \quad (* *')$$

The original estimate $O_f(Nr_1^{-1})$ for the error term can be obtained by simply correcting signs in the calculation on the top of page 921 of [1]; the same idea, but with slightly more careful analysis gives (**'). Without loss of generality $|l - k| \leq N_0$ (otherwise both sides of (**') are 0), and

$$\begin{aligned} \langle f\phi_{2l,2m}, \phi_{2k,2t} \rangle &= \frac{1}{(ir_1 - 2l - 1)(-ir_1 - 2k - 1)} \langle fE_1^- \phi_{2l+2,2m}, E_1^- \phi_{2k+2,2t} \rangle \\ &= \frac{1}{(ir_1 - 2l - 1)(-ir_1 - 2k - 1)} (\langle E_1^- (f\phi_{2l+2,2m}), E_1^- \phi_{2k+2,2t} \rangle \\ &\quad - \langle E_1^- (f)\phi_{2l+2,2m}, E_1^- \phi_{2k+2,2t} \rangle) \\ &= -\frac{1}{(ir_1 - 2l - 1)(-ir_1 - 2k - 1)} (\langle f\phi_{2l+2,2m}, E_1^+ E_1^- \phi_{2k+2,2t} \rangle - O_f(r_1)) \\ &= -\frac{(-ir_1 + 2k + 1)(-ir_1 - 2k - 1)}{(ir_1 - 2l - 1)(-ir_1 - 2k - 1)} \langle f\phi_{2l+2,2m}, \phi_{2k+2,2t} \rangle + O_f(r_1^{-1}) \\ &= \langle f\phi_{2l+2,2m}, \phi_{2k+2,2t} \rangle + O_f(|k - l| r_1^{-1}) + O_f(r_1^{-1}) \\ &= \langle f\phi_{2l+2,2m}, \phi_{2k+2,2t} \rangle + O_f(r_1^{-1}). \end{aligned}$$

This calculation needs to be iterated N times, and not N_0 times as claimed on page 921, which does indeed give

$$\langle f\phi_{2l,2m}, \phi_{2k,2t} \rangle = \langle f\phi_{2l-2k,2m-2t}, \phi_{0,0} \rangle + O_f(N \max(r_1^{-1}, r_2^{-1})),$$

as stated in [1], page 921.

The proof now proceeds as written, with the obvious typo corrected in the formula for Fejer summation: the coefficients of the sum should

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be $\frac{(2N-2|l|+1)(2N-2|m|+1)}{(2N+1)^2}$. Notice that in the same formula the summation is effectively over $|l|, |m| \leq N_0$, and so since the sum is of fixed length the error term remains unchanged.

REFERENCES

- [1] E. Lindenstrauss. On quantum unique ergodicity for $\Gamma \backslash H \times H$. *IMRN*, 17:913–933, 2001.

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